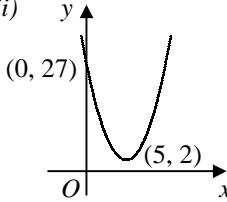


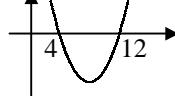
C1 Paper E – Marking Guide

1. (i) $= \frac{21}{\sqrt{7}} \times \frac{\sqrt{7}}{\sqrt{7}} = 3\sqrt{7}$ M1 A1
(ii) $= \frac{1}{\sqrt[3]{8}} = \frac{1}{2}$ M1 A1 (4)

2. (i) $= 1 - 4x$ M1 A1
(ii) $= -6x^{-3}$ M1 A1 (4)

3. (a) $= (x - 5)^2 - 25 + 27$ M1
 $= (x - 5)^2 + 2$ A2
(b) (i) (ii)  B3
(6)

4. (i) $y + 5 = 2(x - 4)$ M1
 $y = 2x - 13$ A1
(ii) $3x - y = 4 \Rightarrow y = 3x - 4 \therefore \text{grad} = 3$
 $\text{grad } l_2 = \frac{-1}{3} = -\frac{1}{3}$ M1 A1
 $\therefore y - 0 = -\frac{1}{3}(x - 3) \quad [y = -\frac{1}{3}x + 1]$ A1
(iii) $2x - 13 = -\frac{1}{3}x + 1$
 $x = 6$ M1 A1
 $\therefore (6, -1)$ A1 (8)

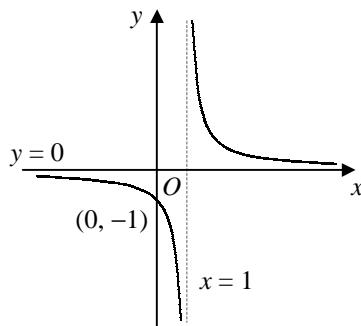
5. (i) real roots $\therefore b^2 - 4ac \geq 0$
 $(-k)^2 - [4 \times 4 \times (k - 3)] \geq 0$ M1
 $k^2 - 16k + 48 \geq 0$ A1
(ii) $(k - 4)(k - 12) \geq 0$ M1
 $k \leq 4 \text{ or } k \geq 12$ M1
 A1
(iii) $k = 4$ B1
 $4x^2 - 4x + 1 = 0$
 $(2x - 1)^2 = 0$ M1
 $x = \frac{1}{2}$ A1 (8)

6. (i) $= (\frac{-2+4}{2}, \frac{6-1}{2}) = (1, \frac{5}{2})$ M1 A1
(ii) radius = dist. $(-2, 6)$ to $(1, \frac{5}{2}) = \sqrt{9 + \frac{49}{4}} = \sqrt{\frac{85}{4}}$ M1 A1
 $\therefore (x - 1)^2 + (y - \frac{5}{2})^2 = (\sqrt{\frac{85}{4}})^2$ M1 A1
 $x^2 - 2x + 1 + y^2 - 5y + \frac{25}{4} = \frac{85}{4}$
 $x^2 + y^2 - 2x - 5y - 14 = 0$ A1
(iii) $(2, 7)$, LHS $= 4 + 49 - 4 - 35 - 14 = 0 \therefore R \text{ lies on circle}$ B1
 $\angle PRQ = 90^\circ$ B1 (9)

7. (i) translation by 1 unit in the positive x -direction

B2

- (ii)



B3

$$(iii) \frac{1}{x-1} = 2 + \frac{1}{x}$$

$$x = 2x(x-1) + (x-1)$$

$$2x^2 - 2x - 1 = 0$$

$$x = \frac{2 \pm \sqrt{4+8}}{4}$$

$$x = \frac{2 \pm 2\sqrt{3}}{4}$$

$$x = \frac{1}{2} \pm \frac{1}{2}\sqrt{3}$$

M1

A1

M1

M1

A1

(10)

8. (i) $x(x^2 + 3x - 4) = 0$
 $x(x + 4)(x - 1) = 0$
 $x = 0$ (at O), -4 , 1
 $\therefore (-4, 0)$, $(1, 0)$

M1

M1

A1

$$(ii) \frac{dy}{dx} = 3x^2 + 6x - 4$$

$$\text{grad} = -4$$

$$\therefore y = -4x$$

$$(iii) x^3 + 3x^2 - 4x = -4x$$

$$x^3 + 3x^2 = 0$$

$$x^2(x + 3) = 0$$

$$x = 0$$
 (at O), -3
 $\therefore (-3, 12)$

M1 A1

M1

A1

M1

M1

A1

(11)

9. (i) $\frac{dy}{dx} = 3x^{\frac{1}{2}} - 4x^{-\frac{1}{2}}$
- $$(ii) 3x^{\frac{1}{2}} - 4x^{-\frac{1}{2}} = 0$$
- $$x^{-\frac{1}{2}}(3x - 4) = 0$$
- $$x = \frac{4}{3}$$

M1 A2

M1

M1

A1

$$(iii) x = 2 \quad \therefore y = 2(2\sqrt{2}) - 8(\sqrt{2}) = -4\sqrt{2}$$

$$\text{grad} = 3\sqrt{2} - \frac{4}{\sqrt{2}} = 3\sqrt{2} - 2\sqrt{2} = \sqrt{2}$$

$$\therefore y + 4\sqrt{2} = \sqrt{2}(x - 2)$$

$$y = \sqrt{2}x - 6\sqrt{2}$$

M1 A1

M1 A1

M1

A1

(12)

Total (72)